# 1 INTRODUCTION

#### INTELLIGENT AGENTS

append *percept* to the end of *percepts action*  $\leftarrow$  LOOKUP(*percepts*, *table*) **return** *action* 

**Figure 2.3** The TABLE-DRIVEN-AGENT program is invoked for each new percept and returns an action each time. It retains the complete percept sequence in memory.

function REFLEX-VACUUM-AGENT([location,status]) returns an action

**if** status = Dirty **then return** Suck **else if** location = A **then return** Right **else if** location = B **then return** Left

**Figure 2.4** The agent program for a simple reflex agent in the two-state vacuum environment. This program implements the agent function tabulated in Figure **??**.

function SIMPLE-REFLEX-AGENT( percept) returns an action
persistent: rules, a set of condition-action rules

 $state \leftarrow INTERPRET-INPUT(percept)$   $rule \leftarrow RULE-MATCH(state, rules)$   $action \leftarrow rule.ACTION$ **return** action

**Figure 2.6** A simple reflex agent. It acts according to a rule whose condition matches the current state, as defined by the percept.

```
function MODEL-BASED-REFLEX-AGENT(percept) returns an action
persistent: state, the agent's current conception of the world state
    model, a description of how the next state depends on current state and action
    rules, a set of condition-action rules
    action, the most recent action, initially none
    state ← UPDATE-STATE(state, action, percept, model)
    rule ← RULE-MATCH(state, rules)
    action ← rule.ACTION
    return action
    Figure 2.8 A model-based reflex agent. It keeps track of the current state of the world, using an
    internal model. It then chooses an action in the same way as the reflex agent.
```

#### SOLVING PROBLEMS BY SEARCHING

```
function SIMPLE-PROBLEM-SOLVING-AGENT(percept) returns an action
persistent: seq, an action sequence, initially empty
```

state, some description of the current world state goal, a goal, initially null problem, a problem formulation

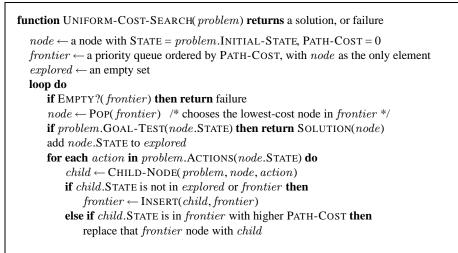
```
state \leftarrow UPDATE-STATE(state, percept)
if seq is empty then
goal \leftarrow FORMULATE-GOAL(state)
problem \leftarrow FORMULATE-PROBLEM(state, goal)
seq \leftarrow SEARCH(problem)
if seq = failure then return a null action
action \leftarrow FIRST(seq)
seq \leftarrow REST(seq)
return action
```

**Figure 3.1** A simple problem-solving agent. It first formulates a goal and a problem, searches for a sequence of actions that would solve the problem, and then executes the actions one at a time. When this is complete, it formulates another goal and starts over.

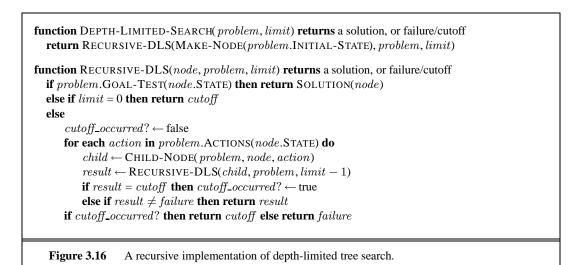
function TREE-SEARCH( <i>problem</i> ) returns a solution, or failure
initialize the frontier using the initial state of <i>problem</i>
loop do
if the frontier is empty then return failure
choose a leaf node and remove it from the frontier
if the node contains a goal state <b>then return</b> the corresponding solution
expand the chosen node, adding the resulting nodes to the frontier
function GRAPH-SEARCH( <i>problem</i> ) returns a solution, or failure
initialize the frontier using the initial state of <i>problem</i>
initialize the explored set to be empty
loop do
if the frontier is empty then return failure
choose a leaf node and remove it from the frontier
if the node contains a goal state then return the corresponding solution
add the node to the explored set
expand the chosen node, adding the resulting nodes to the frontier
only if not in the frontier or explored set
<b>Figure 3.7</b> An informal description of the general tree search and graph search algorithms. T

**Figure 3.7** An informal description of the general tree-search and graph-search algorithms. The parts of GRAPH-SEARCH marked in bold italic are the additions needed to handle repeated states.

function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
$node \leftarrow a \text{ node with } STATE = problem.INITIAL-STATE, PATH-COST = 0$
if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
<i>frontier</i> $\leftarrow$ a FIFO queue with <i>node</i> as the only element
$explored \leftarrow an empty set$
loop do
if EMPTY?(frontier) then return failure
$node \leftarrow POP(frontier) /* chooses the shallowest node in frontier */$
add node.STATE to explored
for each action in problem.ACTIONS(node.STATE) do
$child \leftarrow CHILD$ -NODE( $problem, node, action$ )
if <i>child</i> .STATE is not in <i>explored</i> or <i>frontier</i> then
if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)
$frontier \leftarrow \text{INSERT}(child, frontier)$
Figure 3.11 Breadth-first search on a graph.



**Figure 3.13** Uniform-cost search on a graph. The algorithm is identical to the general graph search algorithm in Figure **??**, except for the use of a priority queue and the addition of an extra check in case a shorter path to a frontier state is discovered. The data structure for *frontier* needs to support efficient membership testing, so it should combine the capabilities of a priority queue and a hash table.



```
function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution, or failure

for depth = 0 to \infty do

result \leftarrow DEPTH-LIMITED-SEARCH(problem, depth)

if result \neq cutoff then return result
```

**Figure 3.17** The iterative deepening search algorithm, which repeatedly applies depth-limited search with increasing limits. It terminates when a solution is found or if the depth-limited search returns *failure*, meaning that no solution exists.

function RECURSIVE-BEST-FIRST-SEARCH( <i>problem</i> ) returns a solution, or failure return RBFS( <i>problem</i> , MAKE-NODE( <i>problem</i> .INITIAL-STATE), $\infty$ )
function RBFS(problem, node, f_limit) returns a solution, or failure and a new f-cost limit
if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
successors $\leftarrow$ []
for each action in problem.ACTIONS(node.STATE) do
add CHILD-NODE(problem, node, action) into successors
if successors is empty then return failure, $\infty$
for each s in successors do /* update f with value from previous search, if any */
$s.f \leftarrow \max(s.g + s.h, node.f))$
loop do
$best \leftarrow the lowest f-value node in successors$
if $best.f > f\_limit$ then return failure, $best.f$
alternative $\leftarrow$ the second-lowest <i>f</i> -value among successors
result, best. $f \leftarrow \text{RBFS}(problem, best, \min(f\_limit, alternative))$
if result $\neq$ failure then return result
Figure 3.24 The algorithm for recursive best-first search.

#### BEYOND CLASSICAL SEARCH

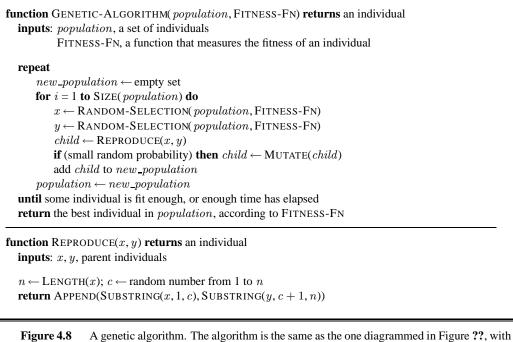
function HILL-CLIMBING(problem) returns a state that is a local maximum

current ← MAKE-NODE(problem.INITIAL-STATE) loop do neighbor ← a highest-valued successor of current if neighbor.VALUE ≤ current.VALUE then return current.STATE current ← neighbor

**Figure 4.2** The hill-climbing search algorithm, which is the most basic local search technique. At each step the current node is replaced by the best neighbor; in this version, that means the neighbor with the highest VALUE, but if a heuristic cost estimate h is used, we would find the neighbor with the lowest h.

 $\begin{aligned} & \textbf{function SIMULATED-ANNEALING}(problem, schedule) \textbf{ returns a solution state} \\ & \textbf{inputs: } problem, a problem \\ & schedule, a mapping from time to "temperature" \\ & current \leftarrow MAKE-NODE(problem.INITIAL-STATE) \\ & \textbf{for } t = 1 \textbf{ to } \infty \textbf{ do} \\ & T \leftarrow schedule(t) \\ & \textbf{if } T = 0 \textbf{ then return } current \\ & next \leftarrow a randomly selected successor of current \\ & \Delta E \leftarrow next.VALUE - current.VALUE \\ & \textbf{if } \Delta E > 0 \textbf{ then } current \leftarrow next \\ & \textbf{else } current \leftarrow next \text{ only with probability } e^{\Delta E/T} \end{aligned}$ 

Figure 4.5 The simulated annealing algorithm, a version of stochastic hill climbing where some downhill moves are allowed. Downhill moves are accepted readily early in the annealing schedule and then less often as time goes on. The *schedule* input determines the value of the temperature T as a function of time.



one variation: in this more popular version, each mating of two parents produces only one offspring, not two.

function OR-SEARCH(state, problem, path) returns a conditional plan, of	or failure
if problem.GOAL-TEST(state) then return the empty plan	
if state is on path then return failure	
for each action in problem.ACTIONS(state) do	
$plan \leftarrow \text{And-Search}(\text{Results}(state, action), problem, [state   particular of the state   pa$	<i>th</i> ])
if $plan \neq failure$ then return $[action \mid plan]$	
return failure	
<b>function</b> AND-SEARCH( <i>states</i> , <i>problem</i> , <i>path</i> ) <b>returns</b> <i>a conditional plan</i> <b>for each</b> <i>s<sub>i</sub></i> <b>in</b> <i>states</i> <b>do</b>	, or failure
$plan_i \leftarrow \text{OR-SEARCH}(s_i, problem, path)$	
if $plan_i = failure$ then return $failure$	
return [if $s_1$ then $plan_1$ else if $s_2$ then $plan_2$ else if $s_{n-1}$ then $plan_n$	$_{-1}$ else $plan_n$ ]

```
function ONLINE-DFS-AGENT(s') returns an action
  inputs: s', a percept that identifies the current state
  persistent: result, a table indexed by state and action, initially empty
               untried, a table that lists, for each state, the actions not yet tried
               unbacktracked, a table that lists, for each state, the backtracks not yet tried
               s, a, the previous state and action, initially null
  if GOAL-TEST(s') then return stop
  if s' is a new state (not in untried) then untried[s'] \leftarrow ACTIONS(s')
  if s is not null then
      result[s, a] \leftarrow s'
      add s to the front of unbacktracked[s']
  if untried[s'] is empty then
      if unbacktracked[s'] is empty then return stop
      else a \leftarrow an action b such that result[s', b] = POP(unbacktracked[s'])
  else a \leftarrow \text{POP}(untried[s'])
  s \leftarrow s'
  return a
```

**Figure 4.21** An online search agent that uses depth-first exploration. The agent is applicable only in state spaces in which every action can be "undone" by some other action.

```
function LRTA*-AGENT(s') returns an action
  inputs: s', a percept that identifies the current state
  persistent: result, a table, indexed by state and action, initially empty
               H, a table of cost estimates indexed by state, initially empty
               s, a, the previous state and action, initially null
  if GOAL-TEST(s') then return stop
  if s' is a new state (not in H) then H[s'] \leftarrow h(s')
  if s is not null
      result[s, a] \leftarrow s'
      H[s] \leftarrow \min_{b \in \text{ACTIONS}(s)} \text{LRTA*-COST}(s, b, result[s, b], H)
  a \leftarrow an action b in ACTIONS(s') that minimizes LRTA*-COST(s', b, result[s', b], H)
  s \gets s'
  return a
function LRTA*-COST(s, a, s', H) returns a cost estimate
  if s' is undefined then return h(s)
  else return c(s, a, s') + H[s']
```

**Figure 4.24** LRTA\*-AGENT selects an action according to the values of neighboring states, which are updated as the agent moves about the state space.

#### ADVERSARIAL SEARCH

```
\begin{array}{l} \textbf{function } \text{MINIMAX-DECISION}(state) \textbf{ returns } an \ action \\ \textbf{return} \ \arg\max_{a \ \in \ \textbf{ACTIONS}(s)} \ \textbf{MIN-VALUE}(\textbf{RESULT}(state, a)) \end{array}
```

```
function MAX-VALUE(state) returns a utility value

if TERMINAL-TEST(state) then return UTILITY(state)

v \leftarrow -\infty

for each a in ACTIONS(state) do

v \leftarrow MAX(v, MIN-VALUE(RESULT(s, a)))

return v
```

```
function MIN-VALUE(state) returns a utility value

if TERMINAL-TEST(state) then return UTILITY(state)

v \leftarrow \infty

for each a in ACTIONS(state) do

v \leftarrow MIN(v, MAX-VALUE(RESULT(s, a)))

return v
```

**Figure 5.3** An algorithm for calculating minimax decisions. It returns the action corresponding to the best possible move, that is, the move that leads to the outcome with the best utility, under the assumption that the opponent plays to minimize utility. The functions MAX-VALUE and MIN-VALUE go through the whole game tree, all the way to the leaves, to determine the backed-up value of a state. The notation  $\operatorname{argmax}_{a \in S} f(a)$  computes the element *a* of set *S* that has the maximum value of f(a).

```
function ALPHA-BETA-SEARCH(state) returns an action
   v \leftarrow \text{MAX-VALUE}(state, -\infty, +\infty)
  return the action in ACTIONS(state) with value v
function MAX-VALUE(state, \alpha, \beta) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow -\infty
  for each a in ACTIONS(state) do
      v \leftarrow Max(v, Min-Value(Result(s, a), \alpha, \beta))
      if v \geq \beta then return v
      \boldsymbol{\alpha} \gets \operatorname{MAX}(\boldsymbol{\alpha}, \, \boldsymbol{v})
   return v
function MIN-VALUE(state, \alpha, \beta) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow +\infty
  for each a in ACTIONS(state) do
      v \leftarrow \text{Min}(v, \text{Max-Value}(\text{Result}(s, a), \alpha, \beta))
       \text{ if } v \ \leq \ \alpha \ \text{ then return } v \\
      \beta \leftarrow MIN(\beta, v)
   return v
```

**Figure 5.7** The alpha–beta search algorithm. Notice that these routines are the same as the MINIMAX functions in Figure **??**, except for the two lines in each of MIN-VALUE and MAX-VALUE that maintain  $\alpha$  and  $\beta$  (and the bookkeeping to pass these parameters along).

#### CONSTRAINT SATISFACTION PROBLEMS

```
function AC-3(csp) returns false if an inconsistency is found and true otherwise inputs: csp, a binary CSP with components (X, D, C) local variables: queue, a queue of arcs, initially all the arcs in csp
while queue is not empty do
```

```
(X_i, X_j) \leftarrow \text{REMOVE-FIRST}(queue)

if REVISE(csp, X_i, X_j) then

if size of D_i = 0 then return false

for each X_k in X_i.NEIGHBORS - \{X_j\} do

add (X_k, X_i) to queue
```

return true

function REVISE( csp,  $X_i$ ,  $X_j$ ) returns true iff we revise the domain of  $X_i$ 

```
revised \leftarrow false

for each x in D_i do

if no value y in D_j allows (x,y) to satisfy the constraint between X_i and X_j then

delete x from D_i

revised \leftarrow true

return revised
```

**Figure 6.3** The arc-consistency algorithm AC-3. After applying AC-3, either every arc is arc-consistent, or some variable has an empty domain, indicating that the CSP cannot be solved. The name "AC-3" was used by the algorithm's inventor (?) because it's the third version developed in the paper.

return BACKTRACK( $\{$   $\}$ , csp) function BACKTRACK(assignment, csp) returns a solution, or failure if assignment is complete then return assignment var  $\leftarrow$  SELECT-UNASSIGNED-VARIABLE(csp) for each value in ORDER-DOMAIN-VALUES(var, assignment, csp) do if value is consistent with assignment then add {var = value} to assignment inferences  $\leftarrow$  INFERENCE(csp, var, value) if inferences  $\neq$  failure then add inferences to assignment result  $\leftarrow$  BACKTRACK(assignment, csp) if result  $\neq$  failure then return result remove {var = value} and inferences from assignment return failure

function BACKTRACKING-SEARCH(csp) returns a solution, or failure

**Figure 6.5** A simple backtracking algorithm for constraint satisfaction problems. The algorithm is modeled on the recursive depth-first search of Chapter **??**. By varying the functions SELECT-UNASSIGNED-VARIABLE and ORDER-DOMAIN-VALUES, we can implement the general-purpose heuristics discussed in the text. The function INFERENCE can optionally be used to impose arc-, path-, or *k*-consistency, as desired. If a value choice leads to failure (noticed either by INFERENCE or by BACKTRACK), then value assignments (including those made by INFERENCE) are removed from the current assignment and a new value is tried.

function MIN-CONFLICTS(csp,  $max\_steps$ ) returns a solution or failure inputs: csp, a constraint satisfaction problem  $max\_steps$ , the number of steps allowed before giving up  $current \leftarrow$  an initial complete assignment for cspfor i = 1 to  $max\_steps$  do if current is a solution for csp then return current  $var \leftarrow$  a randomly chosen conflicted variable from csp.VARIABLES  $value \leftarrow$  the value v for var that minimizes CONFLICTS(var, v, current, csp) set var = value in currentreturn failure

**Figure 6.8** The MIN-CONFLICTS algorithm for solving CSPs by local search. The initial state may be chosen randomly or by a greedy assignment process that chooses a minimal-conflict value for each variable in turn. The CONFLICTS function counts the number of constraints violated by a particular value, given the rest of the current assignment.

```
function TREE-CSP-SOLVER( csp) returns a solution, or failure

inputs: csp, a CSP with components X, D, C

n \leftarrow number of variables in X

assignment \leftarrow an empty assignment

root \leftarrow any variable in X

X \leftarrow TOPOLOGICALSORT(X, root)

for j = n down to 2 do

MAKE-ARC-CONSISTENT(PARENT(X_j), X_j)

if it cannot be made consistent then return failure

for i = 1 to n do

assignment[X_i] \leftarrow any consistent value from D_i

if there is no consistent value then return failure

return assignment
```

**Figure 6.11** The TREE-CSP-SOLVER algorithm for solving tree-structured CSPs. If the CSP has a solution, we will find it in linear time; if not, we will detect a contradiction.

#### LOGICAL AGENTS

TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t)) action  $\leftarrow$  Ask(KB, MAKE-ACTION-QUERY(t)) TELL(KB, MAKE-ACTION-SENTENCE(action, t))  $t \leftarrow t + 1$ **return** action

**Figure 7.1** A generic knowledge-based agent. Given a percept, the agent adds the percept to its knowledge base, asks the knowledge base for the best action, and tells the knowledge base that it has in fact taken that action.

symbols $\leftarrow$ a list of the proposition symbols in KB and $\alpha$ return TT-CHECK-ALL(KB, $\alpha$ , symbols, { })
<b>function</b> TT-CHECK-ALL(KB, $\alpha$ , symbols, model) <b>returns</b> true or false
if Empty?(symbols) then
if PL-TRUE?( <i>KB</i> , <i>model</i> ) then return PL-TRUE?( $\alpha$ , <i>model</i> )
else return true // when KB is false, always return true
else do
$P \leftarrow FIRST(symbols)$
$rest \leftarrow \text{Rest}(symbols)$
<b>return</b> (TT-CHECK-ALL(KB, $\alpha$ , rest, model $\cup \{P = true\}$ )
and
$TT-CHECK-ALL(KB, \alpha, rest, model \ \cup \{P = false \}))$

**Figure 7.8** A truth-table enumeration algorithm for deciding propositional entailment. (TT stands for truth table.) PL-TRUE? returns *true* if a sentence holds within a model. The variable *model* represents a partial model—an assignment to some of the symbols. The keyword "**and**" is used here as a logical operation on its two arguments, returning *true* or *false*.

<b>function</b> PL-RESOLUTION( <i>KB</i> , $\alpha$ ) <b>returns</b> <i>true</i> or <i>false</i> <b>inputs</b> : <i>KB</i> , the knowledge base, a sentence in propositional logic $\alpha$ , the query, a sentence in propositional logic
clauses $\leftarrow$ the set of clauses in the CNF representation of $KB \land \neg \alpha$ new $\leftarrow \{ \}$
loop do
for each pair of clauses $C_i, C_j$ in clauses do resolvents $\leftarrow$ PL-RESOLVE $(C_i, C_j)$
if resolvents contains the empty clause then return true $new \leftarrow new \cup resolvents$
if $new \subseteq clauses$ then return $false$
$clauses \leftarrow clauses \cup new$
Figure 7.9 A simple resolution algorithm for propositional logic. The function PL-RESOLVE re-

turns the set of all possible clauses obtained by resolving its two inputs.

```
function PL-FC-ENTAILS?(KB, q) returns true or false

inputs: KB, the knowledge base, a set of propositional definite clauses

q, the query, a proposition symbol

count \leftarrow a table, where count[c] is the number of symbols in c's premise

inferred \leftarrow a table, where inferred[s] is initially false for all symbols

agenda \leftarrow a queue of symbols, initially symbols known to be true in KB

while agenda is not empty do

p \leftarrow POP(agenda)

if p = q then return true

if inferred[p] = false then

inferred[p] \leftarrow true

for each clause c in KB where p is in c.PREMISE do

decrement count[c]

if count[c] = 0 then add c.CONCLUSION to agenda

return false
```

**Figure 7.12** The forward-chaining algorithm for propositional logic. The *agenda* keeps track of symbols known to be true but not yet "processed." The *count* table keeps track of how many premises of each implication are as yet unknown. Whenever a new symbol p from the agenda is processed, the count is reduced by one for each implication in whose premise p appears (easily identified in constant time with appropriate indexing.) If a count reaches zero, all the premises of the implication are known, so its conclusion can be added to the agenda. Finally, we need to keep track of which symbols have been processed; a symbol that is already in the set of inferred symbols need not be added to the agenda again. This avoids redundant work and prevents loops caused by implications such as  $P \Rightarrow Q$  and  $Q \Rightarrow P$ .

function DPLL-SATISFIABLE?(s) returns true or false
inputs: s, a sentence in propositional logic

 $clauses \leftarrow$  the set of clauses in the CNF representation of s $symbols \leftarrow$  a list of the proposition symbols in s**return** DPLL(*clauses*, *symbols*, { })

function DPLL(clauses, symbols, model) returns true or false

if every clause in *clauses* is true in *model* then return *true* if some clause in *clauses* is false in *model* then return *false*  $P, value \leftarrow FIND-PURE-SYMBOL(symbols, clauses, model)$ if P is non-null then return DPLL(clauses, symbols –  $P, model \cup \{P=value\})$  $P, value \leftarrow FIND-UNIT-CLAUSE(clauses, model)$ if P is non-null then return DPLL(clauses, symbols –  $P, model \cup \{P=value\})$  $P \leftarrow FIRST(symbols); rest \leftarrow REST(symbols)$ return DPLL(clauses, rest, model  $\cup \{P=true\})$  or DPLL(clauses, rest, model  $\cup \{P=false\}))$ 

**Figure 7.14** The DPLL algorithm for checking satisfiability of a sentence in propositional logic. The ideas behind FIND-PURE-SYMBOL and FIND-UNIT-CLAUSE are described in the text; each returns a symbol (or null) and the truth value to assign to that symbol. Like TT-ENTAILS?, DPLL operates over partial models.

function WALKSAT(clauses, p, max\_flips) returns a satisfying model or failure
inputs: clauses, a set of clauses in propositional logic
 p, the probability of choosing to do a "random walk" move, typically around 0.5
 max\_flips, number of flips allowed before giving up
model ← a random assignment of true/false to the symbols in clauses
for i = 1 to max\_flips do
 if model satisfies clauses then return model
 clause ← a randomly selected clause from clauses that is false in model
 with probability p flip the value in model of a randomly selected symbol from clause
 else flip whichever symbol in clause maximizes the number of satisfied clauses
 return failure

**Figure 7.15** The WALKSAT algorithm for checking satisfiability by randomly flipping the values of variables. Many versions of the algorithm exist.

```
function Hybrid-Wumpus-Agent(percept) returns an action
  inputs: percept, a list, [stench, breeze, glitter, bump, scream]
  persistent: KB, a knowledge base, initially the atemporal "wumpus physics"
               t, a counter, initially 0, indicating time
              plan, an action sequence, initially empty
  TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))
  TELL the KB the temporal "physics" sentences for time t
  safe \leftarrow \{[x, y] : ASK(KB, OK_{x,y}^t) = true\}
  if ASK(KB, Glitter^t) = true then
     plan \leftarrow [Grab] + \texttt{PLAN-ROUTE}(current, \{[1,1]\}, safe) + [Climb]
  if plan is empty then
     unvisited \leftarrow \{[x, y] : ASK(KB, L_{x,y}^{t'}) = false \text{ for all } t' \leq t\}
     plan \leftarrow PLAN-ROUTE(current, unvisited \cap safe, safe)
  if plan is empty and ASK(KB, HaveArrow^t) = true then
     possible\_wumpus \leftarrow \{[x, y] : ASK(KB, \neg W_{x,y}) = false\}
     plan \leftarrow PLAN-SHOT(current, possible\_wumpus, safe)
  if plan is empty then // no choice but to take a risk
     not\_unsafe \leftarrow \{[x, y] : Ask(KB, \neg OK_{x, y}^t) = false\}
     plan \leftarrow PLAN-ROUTE(current, unvisited \cap not\_unsafe, safe)
  if plan is empty then
     plan \leftarrow PLAN-ROUTE(current, \{[1, 1]\}, safe) + [Climb]
  action \leftarrow POP(plan)
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t \gets t + 1
  return action
function PLAN-ROUTE(current, goals, allowed) returns an action sequence
  inputs: current, the agent's current position
           goals, a set of squares; try to plan a route to one of them
           allowed, a set of squares that can form part of the route
  problem \leftarrow \text{ROUTE-PROBLEM}(current, goals, allowed)
  return A*-GRAPH-SEARCH(problem)
```

**Figure 7.17** A hybrid agent program for the wumpus world. It uses a propositional knowledge base to infer the state of the world, and a combination of problem-solving search and domain-specific code to decide what actions to take.

```
function SATPLAN(init, transition, goal, T_{max}) returns solution or failure
inputs: init, transition, goal, constitute a description of the problem
T_{max}, an upper limit for plan length
```

```
for t = 0 to T_{\max} do

cnf \leftarrow TRANSLATE-TO-SAT(init, transition, goal, t)

model \leftarrow SAT-SOLVER(cnf)

if model is not null then

return EXTRACT-SOLUTION(model)

return failure
```

Figure 7.19 The SATPLAN algorithm. The planning problem is translated into a CNF sentence in which the goal is asserted to hold at a fixed time step t and axioms are included for each time step up to t. If the satisfiability algorithm finds a model, then a plan is extracted by looking at those proposition symbols that refer to actions and are assigned *true* in the model. If no model exists, then the process is repeated with the goal moved one step later.

## 8 FIRST-ORDER LOGIC

#### INFERENCE IN FIRST-ORDER LOGIC

**function** UNIFY $(x, y, \theta)$  returns a substitution to make x and y identical

- **inputs**: *x*, a variable, constant, list, or compound expression
  - y, a variable, constant, list, or compound expression
  - $\boldsymbol{\theta},$  the substitution built up so far (optional, defaults to empty)

if  $\theta$  = failure then return failure else if x = y then return  $\theta$ else if VARIABLE?(x) then return UNIFY-VAR( $x, y, \theta$ ) else if VARIABLE?(y) then return UNIFY-VAR( $y, x, \theta$ ) else if COMPOUND?(x) and COMPOUND?(y) then return UNIFY(x.ARGS, y.ARGS, UNIFY(x.OP, y.OP,  $\theta$ )) else if LIST?(x) and LIST?(y) then return UNIFY(x.REST, y.REST, UNIFY(x.FIRST, y.FIRST,  $\theta$ )) else return failure

**function** UNIFY-VAR( $var, x, \theta$ ) **returns** a substitution

if  $\{var/val\} \in \theta$  then return UNIFY $(val, x, \theta)$ else if  $\{x/val\} \in \theta$  then return UNIFY $(var, val, \theta)$ else if OCCUR-CHECK?(var, x) then return failure else return add  $\{var/x\}$  to  $\theta$ 

**Figure 9.1** The unification algorithm. The algorithm works by comparing the structures of the inputs, element by element. The substitution  $\theta$  that is the argument to UNIFY is built up along the way and is used to make sure that later comparisons are consistent with bindings that were established earlier. In a compound expression such as F(A, B), the OP field picks out the function symbol F and the ARGS field picks out the argument list (A, B).

function FOL-FC-ASK( $KB, \alpha$ ) returns a substitution or false inputs: *KB*, the knowledge base, a set of first-order definite clauses  $\alpha$ , the query, an atomic sentence local variables: new, the new sentences inferred on each iteration repeat until new is empty  $new \leftarrow \{\}$ for each *rule* in *KB* do  $(p_1 \land \ldots \land p_n \Rightarrow q) \leftarrow STANDARDIZE-VARIABLES(rule)$ for each  $\theta$  such that SUBST $(\theta, p_1 \land \ldots \land p_n) =$  SUBST $(\theta, p'_1 \land \ldots \land p'_n)$ for some  $p'_1, \ldots, p'_n$  in KB $q' \leftarrow \text{SUBST}(\theta, q)$ if q' does not unify with some sentence already in KB or new then add q' to new  $\phi \leftarrow \text{UNIFY}(q', \alpha)$ if  $\phi$  is not *fail* then return  $\phi$ add new to KBreturn false

**Figure 9.3** A conceptually straightforward, but very inefficient, forward-chaining algorithm. On each iteration, it adds to KB all the atomic sentences that can be inferred in one step from the implication sentences and the atomic sentences already in KB. The function STANDARDIZE-VARIABLES replaces all variables in its arguments with new ones that have not been used before.

<pre>function FOL-BC-Ask(KB, query) returns a generator of substitutions return FOL-BC-Or(KB, query, { })</pre>	
generator FOL-BC-OR( <i>KB</i> , <i>goal</i> , $\theta$ ) yields a substitution for each rule ( <i>lhs</i> $\Rightarrow$ <i>rhs</i> ) in FETCH-RULES-FOR-GOAL( <i>KB</i> , <i>goal</i> ) do	
$(lhs, rhs) \leftarrow \text{STANDARDIZE-VARIABLES}((lhs, rhs))$ for each $\theta'$ in FOL-BC-AND(KB, lhs, UNIFY(rhs, goal, $\theta$ )) do	
yield $\theta'$	
generator FOL-BC-AND( <i>KB</i> , goals, $\theta$ ) yields a substitution	
if $\theta = failure$ then return	
else if Length(goals) = 0 then yield $\theta$	
else do	
$first, rest \leftarrow FIRST(goals), REST(goals)$	
for each $\theta'$ in FOL-BC-OR( <i>KB</i> , SUBST( $\theta$ , first), $\theta$ ) do	
for each $\theta''$ in FOL-BC-AND(KB, rest, $\theta'$ ) do	
yield $ heta^{\prime\prime}$	

Figure 9.6 A simple backward-chaining algorithm for first-order knowledge bases.

**procedure** APPEND(*ax*, *y*, *az*, *continuation*)

 $trail \leftarrow \text{GLOBAL-TRAIL-POINTER}()$  **if** ax = [] and UNIFY(y, az) **then** CALL(continuation) RESET-TRAIL(trail)  $a, x, z \leftarrow \text{NEW-VARIABLE}()$ , NEW-VARIABLE(), NEW-VARIABLE() **if** UNIFY( $ax, [a \mid x]$ ) and UNIFY( $az, [a \mid z]$ ) **then** APPEND(x, y, z, continuation)

**Figure 9.8** Pseudocode representing the result of compiling the Append predicate. The function NEW-VARIABLE returns a new variable, distinct from all other variables used so far. The procedure CALL(*continuation*) continues execution with the specified continuation.

### 10 classical planning

```
Init(At(C_1, SFO) \land At(C_2, JFK) \land At(P_1, SFO) \land At(P_2, JFK) \\ \land Cargo(C_1) \land Cargo(C_2) \land Plane(P_1) \land Plane(P_2) \\ \land Airport(JFK) \land Airport(SFO)) \\ Goal(At(C_1, JFK) \land At(C_2, SFO)) \\ Action(Load(c, p, a), \\ PRECOND: At(c, a) \land At(p, a) \land Cargo(c) \land Plane(p) \land Airport(a) \\ EFFECT: \neg At(c, a) \land In(c, p)) \\ Action(Unload(c, p, a), \\ PRECOND: In(c, p) \land At(p, a) \land Cargo(c) \land Plane(p) \land Airport(a) \\ EFFECT: At(c, a) \land \neg In(c, p)) \\ Action(Fly(p, from, to), \\ PRECOND: At(p, from) \land Plane(p) \land Airport(from) \land Airport(to) \\ EFFECT: \neg At(p, from) \land At(p, to)) \\ \end{cases}
```

Figure 10.1 A PDDL description of an air cargo transportation planning problem.

```
 \begin{array}{l} Init(Tire(Flat) \land Tire(Spare) \land At(Flat, Axle) \land At(Spare, Trunk)) \\ Goal(At(Spare, Axle)) \\ Action(Remove(obj, loc), \\ PRECOND: At(obj, loc) \\ EFFECT: \neg At(obj, loc) \land At(obj, Ground)) \\ Action(PutOn(t, Axle), \\ PRECOND: Tire(t) \land At(t, Ground) \land \neg At(Flat, Axle) \\ EFFECT: \neg At(t, Ground) \land At(t, Axle)) \\ Action(LeaveOvernight, \\ PRECOND: \\ EFFECT: \neg At(Spare, Ground) \land \neg At(Spare, Axle) \land \neg At(Spare, Trunk) \\ \land \neg At(Flat, Ground) \land \neg At(Flat, Axle) \land \neg At(Flat, Trunk)) \\ \end{array}
```

Figure 10.2 The simple spare tire problem.

```
\begin{array}{l} Init(On(A, Table) \land On(B, Table) \land On(C, A) \\ \land Block(A) \land Block(B) \land Block(C) \land Clear(B) \land Clear(C)) \\ Goal(On(A, B) \land On(B, C)) \\ Action(Move(b, x, y), \\ \texttt{PRECOND:} On(b, x) \land Clear(b) \land Clear(y) \land Block(b) \land Block(y) \land \\ (b \neq x) \land (b \neq y) \land (x \neq y), \\ \texttt{EFFECT:} On(b, y) \land Clear(x) \land \neg On(b, x) \land \neg Clear(y)) \\ Action(MoveToTable(b, x), \\ \texttt{PRECOND:} On(b, x) \land Clear(b) \land Block(b) \land (b \neq x), \\ \texttt{EFFECT:} On(b, Table) \land Clear(x) \land \neg On(b, x)) \end{array}
```

```
Figure 10.3 A planning problem in the blocks world: building a three-block tower. One solution is the sequence [MoveToTable(C, A), Move(B, Table, C), Move(A, Table, B)].
```

```
\begin{array}{l} Init(Have(Cake))\\ Goal(Have(Cake) \land Eaten(Cake))\\ Action(Eat(Cake)\\ & \\ PRECOND: Have(Cake)\\ & \\ EFFECT: \neg Have(Cake) \land Eaten(Cake))\\ Action(Bake(Cake)\\ & \\ PRECOND: \neg Have(Cake)\\ & \\ EFFECT: Have(Cake))\end{array}
```

Figure 10.7 The "have cake and eat cake too" problem.

```
function GRAPHPLAN(problem) returns solution or failuregraph \leftarrow INITIAL-PLANNING-GRAPH(problem)goals \leftarrow CONJUNCTS(problem.GOAL)nogoods \leftarrow an empty hash tablefor tl = 0 to \infty doif goals all non-mutex in S_t of graph thensolution \leftarrow EXTRACT-SOLUTION(graph, goals, NUMLEVELS(graph), nogoods)if solution \neq failure then return solutionif graph and nogoods have both leveled off then return failuregraph \leftarrow EXPAND-GRAPH(graph, problem)Figure 10.9 The GRAPHPLAN algorithm. GRAPHPLAN calls EXPAND-GRAPH to add a level untileither a solution is found by EXTRACT-SOLUTION, or no solution is possible.
```

#### 1 PLANNING AND ACTING IN THE REAL WORLD

 $\begin{aligned} Jobs(\{AddEngine1 \prec AddWheels1 \prec Inspect1\}, \\ \{AddEngine2 \prec AddWheels2 \prec Inspect2\}) \\ Resources(EngineHoists(1), WheelStations(1), Inspectors(2), LugNuts(500)) \\ Action(AddEngine1, DURATION:30, \\ USE:EngineHoists(1)) \\ Action(AddEngine2, DURATION:60, \\ USE:EngineHoists(1)) \\ Action(AddWheels1, DURATION:30, \\ CONSUME:LugNuts(20), USE: WheelStations(1)) \\ Action(AddWheels2, DURATION:15, \\ CONSUME:LugNuts(20), USE: WheelStations(1)) \\ Action(Inspect_i, DURATION:10, \\ USE:Inspectors(1)) \end{aligned}$ 

**Figure 11.1** A job-shop scheduling problem for assembling two cars, with resource constraints. The notation  $A \prec B$  means that action A must precede action B.

```
\begin{aligned} & Refinement(Go(Home, SFO), \\ & \text{STEPS:} [Drive(Home, SFOLongTermParking), \\ & Shuttle(SFOLongTermParking, SFO)]) \end{aligned}
\begin{aligned} & Refinement(Go(Home, SFO), \\ & \text{STEPS:} [Taxi(Home, SFO)]) \end{aligned}
\begin{aligned} & Refinement(Navigate([a, b], [x, y]), \\ & \text{PRECOND:} \ a = x \ \land \ b = y \\ & \text{STEPS:} []) \end{aligned}
\begin{aligned} & Refinement(Navigate([a, b], [x, y]), \\ & \text{PRECOND:} \ Connected([a, b], [a - 1, b]) \\ & \text{STEPS:} [Left, Navigate([a - 1, b], [x, y])]) \end{aligned}
\begin{aligned} & Refinement(Navigate([a, b], [x, y]), \\ & \text{PRECOND:} \ Connected([a, b], [x, y]), \\ & \text{STEPS:} \ [Right, Navigate([a + 1, b], [x, y])]) \end{aligned}
```

**Figure 11.4** Definitions of possible refinements for two high-level actions: going to San Francisco airport and navigating in the vacuum world. In the latter case, note the recursive nature of the refinements and the use of preconditions.

function HIERARCHICAL-SEARCH(problem, hierarchy) returns a solution, or failure
<i>frontier</i> $\leftarrow$ a FIFO queue with [Act] as the only element
loop do
if EMPTY?( <i>frontier</i> ) then return failure
$plan \leftarrow POP(frontier) /*$ chooses the shallowest plan in frontier */
$hla \leftarrow$ the first HLA in <i>plan</i> , or <i>null</i> if none
<i>prefix</i> , <i>suffix</i> $\leftarrow$ the action subsequences before and after <i>hla</i> in <i>plan</i>
$outcome \leftarrow \text{Result}(problem.Initial-State, prefix)$
if <i>hla</i> is null then /* so <i>plan</i> is primitive and <i>outcome</i> is its result */
if outcome satisfies problem.GOAL then return plan
else for each sequence in REFINEMENTS(hla, outcome, hierarchy) do
$frontier \leftarrow \text{INSERT}(\text{APPEND}(prefix, sequence, suffix), frontier)$
<b>Figure 11.5</b> A breadth-first implementation of hierarchical forward planning search. The initial plan supplied to the algorithm is $[Act]$ . The REFINEMENTS function returns a set of action sequences, one

for each refinement of the HLA whose preconditions are satisfied by the specified state, outcome.

function ANGELIC-SEARCH(problem, hierarchy, initialPlan) returns solution or fail frontier  $\leftarrow$  a FIFO queue with initialPlan as the only element loop do if EMPTY?(frontier) then return fail plan  $\leftarrow$  POP(frontier) /\* chooses the shallowest node in frontier \*/ if REACH<sup>+</sup>(problem.INITIAL-STATE, plan) intersects problem.GOAL then if plan is primitive then return plan /\* REACH<sup>+</sup> is exact for primitive plans \*/ guaranteed  $\leftarrow$  REACH<sup>-</sup>(problem.INITIAL-STATE, plan)  $\cap$  problem.GOAL if guaranteed  $\neq$  { } and MAKING-PROGRESS(plan, initialPlan) then finalState  $\leftarrow$  any element of guaranteed return DECOMPOSE(hierarchy, problem.INITIAL-STATE, plan, finalState) hla  $\leftarrow$  some HLA in plan prefix, suffix  $\leftarrow$  the action subsequences before and after hla in plan for each sequence in REFINEMENTS(hla, outcome, hierarchy) do frontier  $\leftarrow$  INSERT(APPEND(prefix, sequence, suffix), frontier)

function DECOMPOSE(*hierarchy*,  $s_0$ , *plan*,  $s_f$ ) returns a solution

```
solution \leftarrow an empty plan

while plan is not empty do

action \leftarrow \text{REMOVE-LAST}(plan)

s_i \leftarrow a state in REACH<sup>-</sup>(s_0, plan) such that s_f \in \text{REACH}^-(s_i, action)

problem \leftarrow a problem with INITIAL-STATE = s_i and GOAL = s_f

solution \leftarrow \text{APPEND}(\text{ANGELIC-SEARCH}(problem, hierarchy, action), solution)

s_f \leftarrow s_i

return solution
```

**Figure 11.8** A hierarchical planning algorithm that uses angelic semantics to identify and commit to high-level plans that work while avoiding high-level plans that don't. The predicate MAKING-PROGRESS checks to make sure that we aren't stuck in an infinite regression of refinements. At top level, call ANGELIC-SEARCH with [Act] as the *initialPlan*.

```
\begin{array}{l} Actors(A,B) \\ Init(At(A, LeftBaseline) \land At(B, RightNet) \land \\ Approaching(Ball, RightBaseline)) \land Partner(A,B) \land Partner(B,A) \\ Goal(Returned(Ball) \land (At(a, RightNet) \lor At(a, LeftNet)) \\ Action(Hit(actor, Ball), \\ & \\ PRECOND:Approaching(Ball, loc) \land At(actor, loc) \\ & \\ EFFECT:Returned(Ball)) \\ Action(Go(actor, to), \\ & \\ PRECOND:At(actor, loc) \land to \neq loc, \\ & \\ EFFECT:At(actor, to) \land \neg At(actor, loc)) \end{array}
```

**Figure 11.10** The doubles tennis problem. Two actors *A* and *B* are playing together and can be in one of four locations: *LeftBaseline*, *RightBaseline*, *LeftNet*, and *RightNet*. The ball can be returned only if a player is in the right place. Note that each action must include the actor as an argument.

### 12 KNOWLEDGE REPRESENTATION

### 13 QUANTIFYING UNCERTAINTY

Figure 13.1 A decision-theoretic agent that selects rational actions.

### 14 PROBABILISTIC REASONING

```
function ENUMERATION-ASK(X, \mathbf{e}, bn) returns a distribution over X
   inputs: X, the query variable
            e, observed values for variables E
             bn, a Bayes net with variables \{X\} \cup \mathbf{E} \cup \mathbf{Y} / * \mathbf{Y} = hidden \ variables */
   \mathbf{Q}(X) \leftarrow a distribution over X, initially empty
   for each value x_i of X do
       \mathbf{Q}(x_i) \leftarrow \text{ENUMERATE-ALL}(bn. \text{VARS}, \mathbf{e}_{x_i})
            where \mathbf{e}_{x_i} is e extended with X = x_i
   return NORMALIZE(\mathbf{Q}(X))
function ENUMERATE-ALL(vars, e) returns a real number
   if EMPTY?(vars) then return 1.0
   Y \leftarrow \text{FIRST}(vars)
   if Y has value y in e
       then return P(y \mid parents(Y)) \times \text{ENUMERATE-ALL}(\text{REST}(vars), \mathbf{e})
       else return \sum_{y} P(y \mid parents(Y)) \times \text{ENUMERATE-ALL}(\text{REST}(vars), \mathbf{e}_{y})
            where \mathbf{e}_y is \mathbf{e} extended with Y = y
    Figure 14.9
                      The enumeration algorithm for answering queries on Bayesian networks.
```

```
      function ELIMINATION-ASK(X, e, bn) returns a distribution over X

      inputs: X, the query variable

      e, observed values for variables E

      bn, a Bayesian network specifying joint distribution P(X_1, ..., X_n)

      factors \leftarrow []

      for each var in ORDER(bn.VARS) do

      factors \leftarrow [MAKE-FACTOR(var, e)|factors]

      if var is a hidden variable then factors \leftarrow SUM-OUT(var, factors)

      return NORMALIZE(POINTWISE-PRODUCT(factors))
```

function PRIOR-SAMPLE(*bn*) returns an event sampled from the prior specified by *bn* inputs: *bn*, a Bayesian network specifying joint distribution  $P(X_1, ..., X_n)$ 

```
\mathbf{x} \leftarrow an event with n elements
foreach variable X_i in X_1, \ldots, X_n do
\mathbf{x}[i] \leftarrow a random sample from \mathbf{P}(X_i \mid parents(X_i))
return \mathbf{x}
```

**Figure 14.12** A sampling algorithm that generates events from a Bayesian network. Each variable is sampled according to the conditional distribution given the values already sampled for the variable's parents.

```
function REJECTION-SAMPLING(X, e, bn, N) returns an estimate of P(X|e)

inputs: X, the query variable

e, observed values for variables E

bn, a Bayesian network

N, the total number of samples to be generated

local variables: N, a vector of counts for each value of X, initially zero

for j = 1 to N do

\mathbf{x} \leftarrow PRIOR-SAMPLE(bn)

if \mathbf{x} is consistent with e then

\mathbf{N}[x] \leftarrow \mathbf{N}[x]+1 where x is the value of X in \mathbf{x}

return NORMALIZE(N)
```

**Figure 14.13** The rejection-sampling algorithm for answering queries given evidence in a Bayesian network.

```
function LIKELIHOOD-WEIGHTING(X, \mathbf{e}, bn, N) returns an estimate of \mathbf{P}(X|\mathbf{e})
  inputs: X, the query variable
            e, observed values for variables E
            bn, a Bayesian network specifying joint distribution \mathbf{P}(X_1, \ldots, X_n)
            N, the total number of samples to be generated
   local variables: W, a vector of weighted counts for each value of X, initially zero
   for j = 1 to N do
       \mathbf{x}, w \leftarrow \text{WEIGHTED-SAMPLE}(bn, \mathbf{e})
       \mathbf{W}[x] \leftarrow \mathbf{W}[x] + w where x is the value of X in x
   return NORMALIZE(W)
function WEIGHTED-SAMPLE(bn, e) returns an event and a weight
   w \leftarrow 1; \mathbf{x} \leftarrow an event with n elements initialized from e
   foreach variable X_i in X_1, \ldots, X_n do
       if X_i is an evidence variable with value x_i in e
           then w \leftarrow w \times P(X_i = x_i \mid parents(X_i))
            else \mathbf{x}[i] \leftarrow a random sample from \mathbf{P}(X_i \mid parents(X_i))
   return x, w
```

**Figure 14.14** The likelihood-weighting algorithm for inference in Bayesian networks. In WEIGHTED-SAMPLE, each nonevidence variable is sampled according to the conditional distribution given the values already sampled for the variable's parents, while a weight is accumulated based on the likelihood for each evidence variable.

function GIBBS-ASK(X, e, bn, N) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ local variables: N, a vector of counts for each value of X, initially zeroZ, the nonevidence variables in bnx, the current state of the network, initially copied from einitialize x with random values for the variables in Zfor j = 1 to N dofor each  $Z_i$  in Z doset the value of  $Z_i$  in x by sampling from  $\mathbf{P}(Z_i|mb(Z_i))$  $\mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1$  where x is the value of X in xreturn NORMALIZE(N)

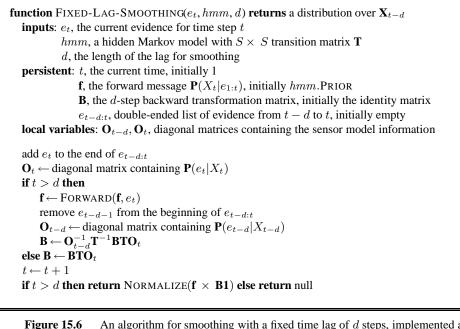
version cycles through the variables, but choosing variables at random also works.

#### 15 PROBABILISTIC REASONING OVER TIME

function FORWARD-BACKWARD(ev, *prior*) returns a vector of probability distributions inputs: ev, a vector of evidence values for steps  $1, \ldots, t$  *prior*, the prior distribution on the initial state,  $P(X_0)$ local variables: fv, a vector of forward messages for steps  $0, \ldots, t$ b, a representation of the backward message, initially all 1s sv, a vector of smoothed estimates for steps  $1, \ldots, t$ fv $[0] \leftarrow prior$ for i = 1 to t do

 $fv[i] \leftarrow FORWARD(fv[i-1], ev[i])$ for i = t downto 1 do  $sv[i] \leftarrow NORMALIZE(fv[i] \times b)$  $b \leftarrow BACKWARD(b, ev[i])$ return sv

**Figure 15.4** The forward–backward algorithm for smoothing: computing posterior probabilities of a sequence of states given a sequence of observations. The FORWARD and BACKWARD operators are defined by Equations (??) and (??), respectively.



**Figure 15.6** An algorithm for smoothing with a fixed time lag of *d* steps, implemented as an online algorithm that outputs the new smoothed estimate given the observation for a new time step. Notice that the final output NORMALIZE( $\mathbf{f} \times \mathbf{B1}$ ) is just  $\alpha \mathbf{f} \times \mathbf{b}$ , by Equation (??).

function PARTICLE-FILTERING(e, N, dbn) returns a set of samples for the next time step inputs: e, the new incoming evidence N, the number of samples to be maintained dbn, a DBN with prior  $P(X_0)$ , transition model  $P(X_1|X_0)$ , sensor model  $P(E_1|X_1)$ persistent: S, a vector of samples of size N, initially generated from  $P(X_0)$ local variables: W, a vector of weights of size N for i = 1 to N do  $S[i] \leftarrow$  sample from  $P(X_1 | X_0 = S[i])$  /\* step 1 \*/  $W[i] \leftarrow P(e | X_1 = S[i])$  /\* step 2 \*/  $S \leftarrow$  WEIGHTED-SAMPLE-WITH-REPLACEMENT(N, S, W) /\* step 3 \*/ return S Figure 15.17 The particle filtering algorithm implemented as a recursive update operation with state

Figure 15.17 The particle filtering algorithm implemented as a recursive update operation with state (the set of samples). Each of the sampling operations involves sampling the relevant slice variables in topological order, much as in PRIOR-SAMPLE. The WEIGHTED-SAMPLE-WITH-REPLACEMENT operation can be implemented to run in O(N) expected time. The step numbers refer to the description in the text.

# $16 \begin{array}{c} {}^{\rm MAKING\ SIMPLE} \\ {}^{\rm DECISIONS} \end{array}$

function INFORMATION-GATHERING-AGENT(*percept*) returns an *action* persistent: *D*, a decision network

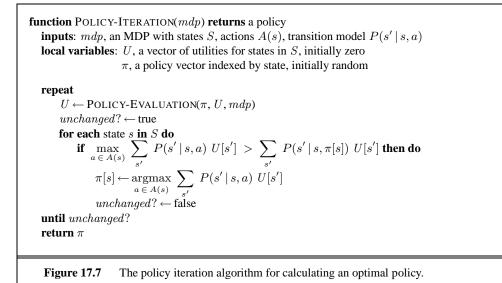
integrate *percept* into D  $j \leftarrow$  the value that maximizes  $VPI(E_j) / Cost(E_j)$ if  $VPI(E_j) > Cost(E_j)$ return REQUEST( $E_j$ ) else return the best action from D

**Figure 16.9** Design of a simple information-gathering agent. The agent works by repeatedly selecting the observation with the highest information value, until the cost of the next observation is greater than its expected benefit.

## 17 MAKING COMPLEX DECISIONS

function VALUE-ITERATION( $mdp, \epsilon$ ) returns a utility function inputs: mdp, an MDP with states S, actions A(s), transition model P(s' | s, a), rewards R(s), discount  $\gamma$   $\epsilon$ , the maximum error allowed in the utility of any state local variables: U, U', vectors of utilities for states in S, initially zero  $\delta$ , the maximum change in the utility of any state in an iteration repeat  $U \leftarrow U'; \delta \leftarrow 0$ for each state s in S do  $U'[s] \leftarrow R(s) + \gamma \max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ if  $|U'[s] - U[s]| > \delta$  then  $\delta \leftarrow |U'[s] - U[s]|$ until  $\delta < \epsilon(1 - \gamma)/\gamma$ return U

**Figure 17.4** The value iteration algorithm for calculating utilities of states. The termination condition is from Equation (**??**).



function POMDP-VALUE-ITERATION( $pomdp, \epsilon$ ) returns a utility function inputs: pomdp, a POMDP with states S, actions A(s), transition model P(s' | s, a), sensor model P(e | s), rewards R(s), discount  $\gamma$   $\epsilon$ , the maximum error allowed in the utility of any state local variables: U, U', sets of plans p with associated utility vectors  $\alpha_p$   $U' \leftarrow a$  set containing just the empty plan [], with  $\alpha_{[]}(s) = R(s)$ repeat  $U \leftarrow U'$   $U' \leftarrow$  the set of all plans consisting of an action and, for each possible next percept, a plan in U with utility vectors computed according to Equation (??)  $U' \leftarrow REMOVE-DOMINATED-PLANS(U')$ until MAX-DIFFERENCE $(U, U') < \epsilon(1 - \gamma)/\gamma$ return U

**Figure 17.9** A high-level sketch of the value iteration algorithm for POMDPs. The REMOVE-DOMINATED-PLANS step and MAX-DIFFERENCE test are typically implemented as linear programs.

## 18 LEARNING FROM EXAMPLES

```
function DECISION-TREE-LEARNING(examples, attributes, parent_examples) returns
tree

if examples is empty then return PLURALITY-VALUE(parent_examples)
else if all examples have the same classification then return the classification
else if attributes is empty then return PLURALITY-VALUE(examples)
```

а

else

 $\begin{array}{l} A \leftarrow \operatorname{argmax}_{a \, \in \, attributes} \, \operatorname{IMPORTANCE}(a, examples) \\ tree \leftarrow a \, \operatorname{new} \, \operatorname{decision} \, \operatorname{tree} \, with \, \operatorname{root} \, \operatorname{test} \, A \\ \textbf{for each} \, \operatorname{value} \, v_k \, \operatorname{of} \, A \, \textbf{do} \\ exs \leftarrow \{e \, : \, e \in examples \, \, \textbf{and} \, \, e.A \, = \, v_k\} \\ subtree \leftarrow \operatorname{DECISION-TREE-LEARNING}(exs, \, attributes - A, examples) \\ \operatorname{add} a \, \operatorname{branch} \, \operatorname{to} \, tree \, \text{with} \, \operatorname{label} \, (A \, = \, v_k) \, \operatorname{and} \, \operatorname{subtree} \, subtree \\ \textbf{return} \, tree \end{array}$ 

**Figure 18.4** The decision-tree learning algorithm. The function IMPORTANCE is described in Section **??**. The function PLURALITY-VALUE selects the most common output value among a set of examples, breaking ties randomly.

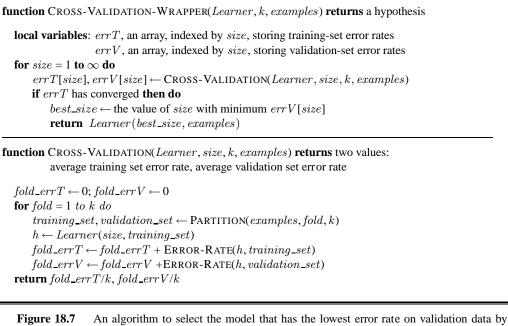


Figure 18.7 An algorithm to select the model that has the lowest error rate on validation data by building models of increasing complexity, and choosing the one with best empirical error rate on validation data. Here errT means error rate on the training data, and errV means error rate on the validation data. Learner(size, examples) returns a hypothesis whose complexity is set by the parameter size, and which is trained on the examples. PARTITION(examples, fold, k) splits examples into two subsets: a validation set of size N/k and a training set with all the other examples. The split is different for each value of fold.

function DECISION-LIST-LEARNING(examples) returns a decision list, or failureif examples is empty then return the trivial decision list No $t \leftarrow$  a test that matches a nonempty subset examples, of examples<br/>such that the members of examples, are all positive or all negativeif there is no such t then return failureif the examples in examples, are positive then  $o \leftarrow Yes$  else  $o \leftarrow No$ return a decision list with initial test t and outcome o and remaining tests given by<br/>DECISION-LIST-LEARNING(examples - examples,<br/>t)Figure 18.10An algorithm for learning decision lists.

```
function BACK-PROP-LEARNING(examples, network) returns a neural network
  inputs: examples, a set of examples, each with input vector x and output vector y
            network, a multilayer network with L layers, weights w_{i,j}, activation function g
  local variables: \Delta, a vector of errors, indexed by network node
  repeat
       for each weight w_{i,j} in network do
           w_{i,j} \leftarrow a \text{ small random number}
      for each example (\mathbf{x}, \mathbf{y}) in examples do
            /* Propagate the inputs forward to compute the outputs */
           for each node i in the input layer do
                a_i \leftarrow x_i
           for \ell = 2 to L do
                for each node j in layer \ell do
                    \begin{array}{l} in_j \leftarrow \sum_i w_{i,j} \ a_i \\ a_j \leftarrow g(in_j) \end{array}
           /* Propagate deltas backward from output layer to input layer */
           for each node j in the output layer do
           \Delta[j] \leftarrow g'(in_j) \times (y_j - a_j)
for \ell = L - 1 to 1 do
                for each node i in layer \ell do
                    \Delta[i] \leftarrow g'(in_i) \sum_j w_{i,j} \Delta[j]
            / * Update every weight in network using deltas * /
           for each weight w_{i,j} in network do
               w_{i,j} \leftarrow w_{i,j} + \alpha \times a_i \times \Delta[j]
  until some stopping criterion is satisfied
  return network
   Figure 18.23
                       The back-propagation algorithm for learning in multilayer networks.
```

```
function ADABOOST(examples, L, K) returns a weighted-majority hypothesis
  inputs: examples, set of N labeled examples (x_1, y_1), \ldots, (x_N, y_N)
            L, a learning algorithm
            K, the number of hypotheses in the ensemble
  local variables: w, a vector of N example weights, initially 1/N
                      h, a vector of K hypotheses
                      z, a vector of K hypothesis weights
  for k = 1 to K do
       \mathbf{h}[k] \leftarrow L(examples, \mathbf{w})
       \mathit{error} \gets 0
       for j = 1 to N do
            if \mathbf{h}[k](x_j) \neq y_j then error \leftarrow error + \mathbf{w}[j]
       for j = 1 to N do
           if \mathbf{h}[k](x_j) = y_j then \mathbf{w}[j] \leftarrow \mathbf{w}[j] \cdot error/(1 - error)
       \mathbf{w} \leftarrow \text{NORMALIZE}(\mathbf{w})
       \mathbf{z}[k] \leftarrow \log (1 - error) / error
   return WEIGHTED-MAJORITY(h, z)
```

**Figure 18.33** The ADABOOST variant of the boosting method for ensemble learning. The algorithm generates hypotheses by successively reweighting the training examples. The function WEIGHTED-MAJORITY generates a hypothesis that returns the output value with the highest vote from the hypotheses in **h**, with votes weighted by **z**.

## 19 KNOWLEDGE IN LEARNING

```
function CURRENT-BEST-LEARNING(examples, h) returns a hypothesis or fail

if examples is empty then

return h

e \leftarrow FIRST(examples)

if e is consistent with h then

return CURRENT-BEST-LEARNING(REST(examples), h)

else if e is a false positive for h then

for each h' in specializations of h consistent with examples seen so far do

h'' \leftarrow CURRENT-BEST-LEARNING(REST(examples), h')

if h'' \neq fail then return h''

else if e is a false negative for h then

for each h' in generalizations of h consistent with examples seen so far do

h'' \leftarrow CURRENT-BEST-LEARNING(REST(examples), h')

if h'' \neq fail then return h''

return fail

then return h''
```

**Figure 19.2** The current-best-hypothesis learning algorithm. It searches for a consistent hypothesis that fits all the examples and backtracks when no consistent specialization/generalization can be found. To start the algorithm, any hypothesis can be passed in; it will be specialized or gneralized as needed.

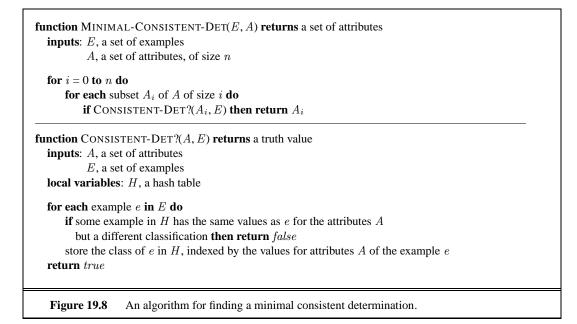
**function** VERSION-SPACE-LEARNING(*examples*) **returns** a version space **local variables**: *V*, the version space: the set of all hypotheses

 $V \leftarrow$  the set of all hypotheses for each example e in examples do if V is not empty then  $V \leftarrow$  VERSION-SPACE-UPDATE(V, e) return V

function VERSION-SPACE-UPDATE(V, e) returns an updated version space

 $V \leftarrow \{h \in V : h \text{ is consistent with } e\}$ 

Figure 19.3 The version space learning algorithm. It finds a subset of V that is consistent with all the *examples*.



Dente Forr	
	mples, target) returns a set of Horn clauses as, set of examples
	literal for the goal predicate
-	clauses, set of clauses, initially empty
iocal variables.	ciauses, set of clauses, initially empty
while examples	contains positive examples do
$clause \leftarrow NH$	EW-CLAUSE( <i>examples</i> , <i>target</i> )
remove posit	ive examples covered by <i>clause</i> from <i>examples</i>
add clause to	o clauses
return clauses	
unction New-CL	AUSE( <i>examples</i> , <i>target</i> ) <b>returns</b> a Horn clause
	clause, a clause with <i>target</i> as head and an empty body
	l, a literal to be added to the clause
	extended_examples, a set of examples with values for new variables
extended_exam	$ples \leftarrow examples$
	examples contains negative examples <b>do</b>
	-LITERAL(NEW-LITERALS(clause), extended_examples)
	ne body of <i>clause</i>
	$amples \leftarrow$ set of examples created by applying EXTEND-EXAMPLE
	ample in <i>extended_examples</i>
return clause	
unction Extend-	EXAMPLE( <i>example</i> , <i>literal</i> ) <b>returns</b> a set of examples
if example satisf	•
*	the set of examples created by extending <i>example</i> with
	ble constant value for each new variable in <i>literal</i>
else return the e	
	••
Figure 19.12	Sketch of the FOIL algorithm for learning sets of first-order Horn clauses from exam-
0	ERALS and CHOOSE-LITERAL are explained in the text.

# 20 LEARNING PROBABILISTIC MODELS

#### 21 REINFORCEMENT LEARNING

function PASSIVE-ADP-AGENT(percept) returns an action **inputs**: *percept*, a percept indicating the current state s' and reward signal r'**persistent**:  $\pi$ , a fixed policy mdp, an MDP with model P, rewards R, discount  $\gamma$ U, a table of utilities, initially empty  $N_{sa}$ , a table of frequencies for state-action pairs, initially zero  $N_{s'|sa}$ , a table of outcome frequencies given state-action pairs, initially zero s, a, the previous state and action, initially null if s' is new then  $U[s'] \leftarrow r'$ ;  $R[s'] \leftarrow r'$ if s is not null then increment  $N_{sa}[s, a]$  and  $N_{s'|sa}[s', s, a]$ for each t such that  $N_{s'|sa}[t, s, a]$  is nonzero do  $P(t \mid s, a) \leftarrow N_{s' \mid sa}[t, s, a] / N_{sa}[s, a]$  $U \leftarrow \text{POLICY-EVALUATION}(\pi, U, mdp)$ if s'.TERMINAL? then  $s, a \leftarrow$  null else  $s, a \leftarrow s', \pi[s']$ return a

**Figure 21.2** A passive reinforcement learning agent based on adaptive dynamic programming. The POLICY-EVALUATION function solves the fixed-policy Bellman equations, as described on page **??**.

function PASSIVE-TD-AGENT(percept) returns an action inputs: percept, a percept indicating the current state s' and reward signal r' persistent:  $\pi$ , a fixed policy U, a table of utilities, initially empty  $N_s$ , a table of frequencies for states, initially zero s, a, r, the previous state, action, and reward, initially null if s' is new then  $U[s'] \leftarrow r'$ if s is not null then increment  $N_s[s]$   $U[s] \leftarrow U[s] + \alpha(N_s[s])(r + \gamma U[s'] - U[s])$ if s'.TERMINAL? then s, a,  $r \leftarrow$  null else s, a,  $r \leftarrow s'$ ,  $\pi[s']$ , r'return a

**Figure 21.4** A passive reinforcement learning agent that learns utility estimates using temporal differences. The step-size function  $\alpha(n)$  is chosen to ensure convergence, as described in the text.

**function** Q-LEARNING-AGENT(*percept*) **returns** an action **inputs**: *percept*, a percept indicating the current state s' and reward signal r' **persistent**: Q, a table of action values indexed by state and action, initially zero  $N_{sa}$ , a table of frequencies for state-action pairs, initially zero s, a, r, the previous state, action, and reward, initially null **if** TERMINAL?(s) **then**  $Q[s, None] \leftarrow r'$  **if** s is not null **then** increment  $N_{sa}[s, a]$   $Q[s, a] \leftarrow Q[s, a] + \alpha(N_{sa}[s, a])(r + \gamma \max_{a'} Q[s', a'] - Q[s, a])$   $s, a, r \leftarrow s'$ ,  $\operatorname{argmax}_{a'} f(Q[s', a'], N_{sa}[s', a']), r'$ **return** a

**Figure 21.8** An exploratory Q-learning agent. It is an active learner that learns the value Q(s, a) of each action in each situation. It uses the same exploration function f as the exploratory ADP agent, but avoids having to learn the transition model because the Q-value of a state can be related directly to those of its neighbors.

## 22 NATURAL LANGUAGE PROCESSING

```
function HITS(query) returns pages with hub and authority numbers
```

```
pages \leftarrow \text{EXPAND-PAGES}(\text{RELEVANT-PAGES}(query))
for each p in pages do
p.AUTHORITY \leftarrow 1
p.HUB \leftarrow 1
repeat until convergence do
for each p in pages do
p.AUTHORITY \leftarrow \sum_i \text{INLINK}_i(p).\text{HUB}
p.HUB \leftarrow \sum_i \text{OUTLINK}_i(p).\text{AUTHORITY}
NORMALIZE(pages)
return pages
```

**Figure 22.1** The HITS algorithm for computing hubs and authorities with respect to a query. RELEVANT-PAGES fetches the pages that match the query, and EXPAND-PAGES adds in every page that links to or is linked from one of the relevant pages. NORMALIZE divides each page's score by the sum of the squares of all pages' scores (separately for both the authority and hubs scores).

### 23 NATURAL LANGUAGE FOR COMMUNICATION

function CYK-PARSE(words, grammar) returns P, a table of probabilities  $N \leftarrow \text{Length}(words)$  $M \leftarrow$  the number of nonterminal symbols in grammar  $P \leftarrow$  an array of size [M, N, N], initially all 0 / \* Insert lexical rules for each word \* / for i = 1 to N do for each rule of form  $(X \rightarrow words_i [p])$  do  $P[X, i, 1] \leftarrow p$ /\* Combine first and second parts of right-hand sides of rules, from short to long \*/ for length = 2 to N do for start = 1 to N - length + 1 do for len1 = 1 to N - 1 do  $len2 \leftarrow length - len1$ for each rule of the form  $(X \rightarrow Y Z [p])$  do  $P[X, start, length] \leftarrow MAX(P[X, start, length]),$  $P[Y, start, len1] \times P[Z, start + len1, len2] \times p)$ 

return P

**Figure 23.4** The CYK algorithm for parsing. Given a sequence of words, it finds the most probable derivation for the whole sequence and for each subsequence. It returns the whole table, P, in which an entry P[X, start, len] is the probability of the most probable X of length *len* starting at position *start*. If there is no X of that size at that location, the probability is 0.

```
[ [S [NP-SBJ-2 Her eyes]

[VP were

[VP glazed

[NP *-2]

[SBAR-ADV as if

[S [NP-SBJ she]

[VP did n't

[VP [VP hear [NP *-1]]

or

[VP [ADVP even] see [NP *-1]]

[NP-1 him]]]]]]]
```

**Figure 23.5** Annotated tree for the sentence "Her eyes were glazed as if she didn't hear or even see him." from the Penn Treebank. Note that in this grammar there is a distinction between an object noun phrase (NP) and a subject noun phrase (NP-SBJ). Note also a grammatical phenomenon we have not covered yet: the movement of a phrase from one part of the tree to another. This tree analyzes the phrase "hear or even see him" as consisting of two constituent VPs, [VP hear [NP \*-1]] and [VP [ADVP even] see [NP \*-1]], both of which have a missing object, denoted \*-1, which refers to the NP labeled elsewhere in the tree as [NP-1 him].

## 24 PERCEPTION

### 25 robotics

```
function MONTE-CARLO-LOCALIZATION(a, z, N, P(X'|X, v, \omega), P(z|z^*), m) returns
a set of samples for the next time step
  inputs: a, robot velocities v and \omega
           z, range scan z_1, \ldots, z_M
           P(X'|X, v, \omega), motion model
           P(z|z^*), range sensor noise model
           m, 2D map of the environment
  persistent: S, a vector of samples of size N
  local variables: W, a vector of weights of size N
                    S', a temporary vector of particles of size N
                    W', a vector of weights of size N
   if S is empty then
                             /* initialization phase */
       for i = 1 to N do
           S[i] \leftarrow \text{sample from } P(X_0)
       for i = 1 to N do /* update cycle */
           S'[i] \leftarrow \text{sample from } P(X'|X = S[i], v, \omega)
           W'[i] \leftarrow 1
           for j = 1 to M do
               z^* \leftarrow \operatorname{RayCast}(j, X = S'[i], m)
               W'[i] \leftarrow W'[i] \cdot P(z_j \mid z^*)
       S \leftarrow \text{Weighted-Sample-With-Replacement}(N, S', W')
   return S
```

**Figure 25.9** A Monte Carlo localization algorithm using a range-scan sensor model with independent noise.

# 26 PHILOSOPHICAL FOUNDATIONS

# 

# 28 MATHEMATICAL BACKGROUND

#### 29 NOTES ON LANGUAGES AND ALGORITHMS

generator POWERS-OF-2() yields ints  $i \leftarrow 1$ while true do yield i $i \leftarrow 2 \times i$ 

for p in POWERS-OF-2() do PRINT(p)

Figure 29.1 Example of a generator function and its invocation within a loop.