## CHI-SQUARE GOODNESS OF FIT TEST

This test is used to determine if observed counts are equal to a hypothesized distribution.
A researcher believes the Mars Company is misleading the public on its color distribution of M\&Ms.
He wants to compare the color distribution from a random sample of M\&Ms to the Mars Company's expected values:

|  | Brown | Red | Yellow | Green | Orange | Blue | Purple |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sample | 4 | 4 | 16 | 10 | 8 | 4 | 4 |
| Expected | $.10(5)$ | $.20(10)$ | $.20(10)$ | $.10(5)$ | $.10(5)$ | $.10(5)$ | $.20(10)$ |

## H STATE NULL AND ALTERNATIVE HYPOTHESES:

$\mathrm{H}_{0}$ : Color distribution of M\&Ms is the same as the company claims
$\mathrm{H}_{\mathrm{a}}$ : Color distribution of M\&Ms is different than the company claims

## A DETERMINE THAT CONDITIONS FOR TEST ARE ACCEPTABLE:

- Counts (not percents)- yes
- Every expected count $\geq 1$ and $80 \% \geq 5$ - yes

PERFORM TEST:
a) Calculate Chi-Square statistic:

$$
X^{2}=\Sigma\left(\mathrm{O}_{\mathrm{i}}-\mathrm{E}_{\mathrm{i}}\right)^{2} / \mathrm{E}_{\mathrm{i}}=(4-5)^{2} / 5+\ldots+(4-10)^{2} / 10=18.0
$$

b) Determine Degrees of Freedom $=$ Number of Categories $-1=7-1=6$
c) Determine P-Value
i) Using Table:

P -value $<.01$ for $\mathrm{X}^{2}$ of 18 and degrees of freedom 6
ii) Using calculator:

DISTR $\rightarrow 7: \mathrm{X}^{2} \operatorname{cdf}(18,100,6) \rightarrow \mathrm{p}=.006$

## S STATE CONCLUSION IN CONTEXT

There is very good evidence to reject $\mathrm{H}_{\mathrm{o}}(\mathrm{p}=.006)$ and conclude that the color distribution of M\&Ms is not what the company claims it should be.

